Roll No.			Candidates must write the Set No. on		
	•	•			the title page of the answer book

SAHODAYA PRE BOARD EXAMINATION - 2023-24

- Please check that this question paper contains **07** printed pages.
- Set number given on the right-hand side of the question paper should be written on the title page of the answer book by the candidates.
- Check that this question paper contains **38** questions.
- Write down the Serial Number of the question in the left side of the margin before attempting it.
- 15 minutes time has been allotted to read this question paper. The question paper will be distributed 15 minutes prior to the commencement of the examination. The students will read the question paper only and will not write any answer on the answer script during this period. Students should not write anything in the question paper.

CLASS-XII

SUB: MATHEMATICS (041)

Time Allowed: 3 Hours Maximum Marks: 70

General Instructions:

- 1. This Question paper contains five sections A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
- 2. Section A has 18 MCQ's and 02 Assertion-Reason based questions of 1 mark each.
- 3. Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
- 4. Section C has 6 Short Answer (SA)-type questions of 3 marks each.
- 5. Section D has 4 Long Answer (LA)-type questions of 5 marks each.
- 6. Section E has 3 source based/case based/passage based/integrated units of assessment (4 marks each) with sub parts.

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SECTION-A

All questions are compulsory. In case of internal choices attempt any one.

1. Let A be a skew-symmetric matrix of order 3. If |A| = x, then $(2023)^x$ is equal to:

(a)2023

(d)1

2. If $A = \begin{bmatrix} \alpha & 2 \\ 2 & \alpha \end{bmatrix}$ and $|A^3| = 125$, the value of α is

(b) 0

 $(c) \pm 1$

(d) ± 3

3. If $\begin{vmatrix} 5 & 3 & -1 \\ -7 & x & -3 \\ 9 & 6 & -2 \end{vmatrix} = 0$ then the value of x is

4. The value of f(0) so that $f(x) = \frac{-e^x + 2^x}{x}$ may be continuous at x = 0 is

(a) $\log\left(\frac{1}{2}\right)$

(d) $-1 + \log 2$

5. If the lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{4-z}{k}$ and $x = 1, \frac{y+1}{2} = \frac{z-1}{-3}$ are mutually perpendicular then the value of k is

(a) 2

(b) 2/3

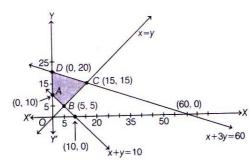
(c) - 2/3

6. Integrating factor of the differential equation $x \frac{dy}{dx} - y = x^5 - 3x^2$ is

(a) x

(d) -x

7. Based on the given shaded region as the feasible region in the graph, at which point(s), the objective function Z = 3x+9y is maximum?



(a) Point B

(b) Point C

(c) Point D

(d) Every point on the line segment CD

8. If $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$, then

(a) $\vec{a} \parallel \vec{b}$ (b) $\vec{a} \perp \vec{b}$

(c) $|\vec{a}| = |\vec{b}|$

(d) None of these

9. If $\int_0^a \frac{1}{1+4x^2} dx = \frac{\pi}{8}$, then "a" is

(a) 1

(c) 3

(d) 2

10. If $A = \begin{bmatrix} \alpha & \beta \\ \gamma & -\alpha \end{bmatrix}$ is such	that $A^2 = I$ then									
$(a) 1 + \alpha^2 + \beta \gamma = 0$		$(b) 1 - \alpha^2 + \beta = 0$								
(c) $1 - \alpha^2 - \beta \gamma = 0$		$(d) 1 + \alpha^2 - \beta \gamma = 0$								
11. Corner points of the fe	asible region is detern	nined by the system of	f linear constraints are (0, 3), (1, 1),							
(3,0). Let $Z = px + q$	y, where $p, q > 0$, cond	dition on p , q so that tl	ne minimum of Z occurs at (3, 0) and							
(1, 1) is										
(a) p=2q	(b) p=q/2	(c) p=3q	(d) p = q							
12. If a line makes an angle $\frac{\pi}{3}$ with each X and Y axes then the obtuse angle made with Z axis is										
(a) $\frac{3\pi}{2}$	(b) $\frac{2\pi}{3}$	$(c)\frac{3\pi}{4}$	$(d)\frac{5\pi}{6}$							
13. If A is a square matrix of order 3, such that A (adj A) = $10I$, then adj A is equal to										
(a) 1	(b) 10	(c) 100	(d) 101							
14.If A and B are two events	14.If A and B are two events such that $P(A)=1/2$, $P(B)=1/3$, and $P(A/B)=1/4$, then $P(A' \cap B')$ is									
(a) 1/12	(b) 3/4	(c) 1/4	(d) 3/16							
15. If a and b are order and degree of the differential equation										
$\left(y\frac{dy}{dx}+x^3\big(\frac{d^2y}{dx^2}\big)\right)^2+$	xy = cosx, then									
(a) $a < b$	(b) $a = b$	(c) $a > b$	(d) none of these							
16. The direction cosines of	vector \overrightarrow{BA} , where coordinates	dinates of A and B are	(1, 2, -1) and $(3, 4, 0)$							
respectively, are:										
(a)-2,-2,-1	(b) $-\frac{2}{3}$, $-\frac{2}{3}$, $-\frac{1}{3}$	(c) 2, 2, 1	$(d) \frac{2}{3}, \frac{2}{3}, \frac{1}{3}$							
17. If $y = \sec x^0$, then $\frac{dy}{dx}$ is equal to :										
(a) sec x tan x	(b) sec x° tan x°	(c) $\frac{\pi}{180}$ sec x° tan x°	(d) None of these							
18. The number of lines pass	sing through the origin	which make equal ang	les with the coordinate axes is							
(a) 1	(b) 4	(c) 8	(d) 2							
ASSERTION-REASON BASED QUESTIONS										
In the following two questions, a statement of assertion (A) is followed by a statement of Reason (R).										
Choose the correct answer out of the following choices.										
(a) Both A and R are true and R is the correct explanation of A.										
(b) Both A and R are true but R is not the correct explanation of A.										
(c) A is true but R is false.										
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- (d) A is false but R is true.
- 19. **Assertion** (A): Let $A = \{-1,1,2,3\}$ and $B = \{1,4,9\}$, where $f: A \to B$ given by $f(x) = x^2$, then f is a many-one function.
 - **Reason** (**R**): If $x_1 \neq x_2 \Rightarrow f(x_1) \neq f(x_2)$, for every $x_1, x_2 \in$ domain, then f is one-one or else manyone.
- 20. **Assertion (A):** The two positive numbers x and y are such that x+y=35 and x^2y^5 is maximum, then the numbers are 10 and 25.
 - **Reason(R):** If f be a function, defined on an interval I and $c \in I$ and also, if f be twice differentiable at c, then x=c is a point of local maximum if f'(c) = 0 and f''(c) < 0 and the value of f(c) is local maximum value of f.

SECTION B

This section comprises of very short answer type-questions (VSA) of 2 marks each

21. Find the domain of $f(x) = \sin^{-1} \sqrt{x-1}$.

OR

Find the value of $sin(2 tan^{-1}(0.75))$.

- 22. If the area of a circle increases at a uniform rate, then prove that the perimeter varies inversely as the radius.
- 23. Find the maximum value of the function $f(x) = \sin x + \cos x$.

OR

A particle moves along the curve $\frac{x^2}{16} + \frac{y^2}{4} = 1$. Find the co-ordinates of the points, where the rate of change of abscissa is 4 times that of its ordinate.

- 24. Evaluate $\int_0^1 \sin^{-1} x dx$
- 25. Divide 64 into two parts such that sum of the cubes of two parts is minimum.

SECTION C

(This section comprises of short answer type questions (SA) of 3 marks each)

26. Evaluate:
$$\int \frac{x+3}{\sqrt{5-4x+x^2}} dx.$$

- 27. Two defective bulbs are accidentally mixed with 6 good ones. If three bulbs are drawn at random, find the mean of the number of defective bulbs drawn.
- 28. Evaluate: $\int \{ \log (\log x) + \frac{1}{(\log x)^2} \} dx$

OR

Evaluate : $\int_0^4 (|x| + |x - 2| + |x - 4|) dx$

29. Solve $(1 + e^{x/y})dx + e^{\frac{x}{y}}(1 - \frac{x}{y})dy = 0$

OR

Solve $\frac{dy}{dx} = \sec(x + y)$

30. Solve the following linear programming problem Minimize Z = 3x + 5y subject to constraints.

$$x + 3y \ge 3$$
, $x + y \ge 2$, $x \ge 0$, $y \ge 0$

OR

Solve the following linear programming problem Maximize Z = -x + 2y subject to constraints.

$$-x + 3y \le 0$$
, $x + y \le 6$, $x - y \le 2$, $x \ge 0$, $y \ge 0$

31. If $x=a(2\theta - \sin 2\theta)$ and $y=a(1-\cos 2\theta)$, find $\frac{d^2y}{dx^2}$ at $\theta = \frac{\pi}{3}$.

SECTION D

(This section comprises of long answer-type questions (LA) of 5 marks each)

- 32. Find the area of the region $\{(x, y): 0 \le y \le x^2 + 1, 0 \le y \le x + 1, 0 \le x \le 2\}$.
- 33. If $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{bmatrix}$, $6A^{-1} = A^2 + cA + dI$ then find the value of (c, d).
- 34. Prove that the relation R on the set N×N defined by (a,b) R (c,d) iff ad(b+c) = bc(a+d) for all (a,b), (c,d) \in $N \times N$ is an equivalence relation.

OR

Let $f: R_+ \to [-5, \infty)$ be a function defined as $f(x) = 9x^2 + 6x - 5$. Show that f is bijective.

35. Find the image of the point (1, 6,3) in the line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$. Also, write the equation of the line joining the given point and its image and find the length of the segment joining the given point and its image.

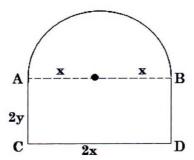
OR

Show that the line $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ and $\frac{x-4}{5} = \frac{y-1}{2} = z$ intersect. Also find the equation of a line passing through the point of intersection of the above lines and parallel to z - axis.

SECTION E

(This section comprises of 3 case-study/passage-based questions 4 marks each with two sub-parts. First two case study questions have three sub-parts (i), (ii), (iii) of marks 1, 1, 2 respectively. The third case study question has two sub-parts of 2 marks each.)

36. Case-Study 1: Read the following passage and answer the questions given below.



Mr Shashi, who is an architect, designs a building for a small company.

The design of window on the ground floor is proposed to be different from other floors.

The window is in the shape of a rectangle which is surmounted by a semi-circular opening.

This window is having a perimeter of 10 m.

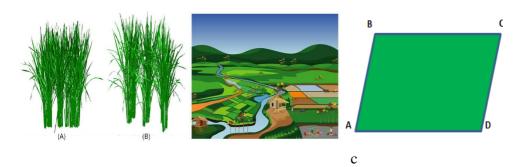
- (i) If 2x and 2y represents the length and breadth of the rectangular portion of the windows then, find the value of y, in terms of x.
- (ii) Express the combined area (A) of the rectangular region and semi-circular region of the window, as a function of x.
- (iii) Find the maximum value of area A of the whole window using derivatives.

OR

(iii) The owner of this small company is interested in maximizing the area of the whole window so that maximum light input is possible. For this to happen, find the length and breadth of rectangular portion of the window. Also find the radius of semi-circular opening of the window. Use derivatives.

37. Case-Study2::

SURVEY BY AGRICULTURE DEPARTMENT



During a survey of Paddy fields in a village, agriculture officers went to a field in the shape of a parallelogram. When they measured the length of the adjacent sides of the paddy field, the results were as $\overrightarrow{AB} = 2\hat{\imath} - 4\hat{\jmath} + 5\hat{k}$ and $\overrightarrow{AD} = \hat{\imath} - 2\hat{\jmath} - 3\hat{k}$.

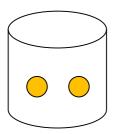
Based on the above situation, answer the following:

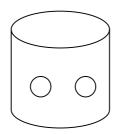
- (i) If one officer, Mr. X, is standing at A (in one corner of the field) and another officer, Mr. Y, is standing at C,(the opposite corner) then find the resultant vector, \overrightarrow{AC} , between them.
- (ii) If Mr. X is walking parallelly to Mr. Y, and Mr. Y is walking along the \overrightarrow{AC} , then find the direction of the unit vector of Mr. X
- (iii) If Mr. X and Mr. Y together covered the entire field, then find the total area covered by them.

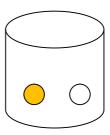
OR

One of the rice stalk's tips was at coordinate P(2,3,4) and the stalk touches the ground at coordinate Q (4,1,-2). In order to collect the rice grains, the stalk has to be divided into exactly two halves. Then find the position vector of point at which it will be divided.

38. **Case-Study 3:** Given three identical boxes I, II and III, each containing two coins. Inbox I, both coins are gold coins, in box II, both are silver coins and, in the box III, there is one gold and one silver coin. A person chooses a box at random and takes out a coin.







Basing on the above concept answer the following

- (i) Find the probability of getting a gold coin?
- (ii) Find the probability of getting a silver coin?

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